



PROGRESSION IN WRITTEN MULTIPLICATION

Pre-learning 1

Practical and informal written methods using concrete objects and pictorial representations

(see Models and Images poster)

Arrays

Use real objects to demonstrate arrays and count in groups:



$$2 \times 6 = 12$$

$$3 \times 4 = 12$$

Repeated addition

Place objects into equal groups:

$$2 \times 3 = 6$$



Multiplication tables

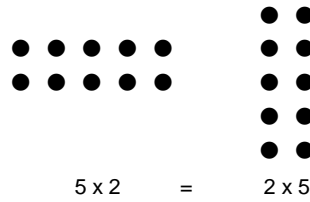
Count in 2s, 5s and 10s

Pre-learning 2

UxU using concrete objects, pictorial representations and mentally

Arrays

(model using counters, peg boards and real objects)



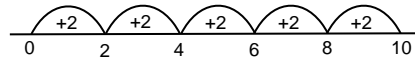
$$5 \times 2 = 2 \times 5$$

Repeated addition

(model on a bead string, number line and peg board)

$$2 \times 5 = 10$$

$$2 \times 5 = 2 + 2 + 2 + 2 + 2$$



$$5 \times 2 = 10$$

$$5 \times 2 = 5 + 5$$



Multiplication tables

2, 5 and 10 multiplication tables modelled as arrays and repeated addition on a number line and practised using rhythm, songs and games.

Make connections between the tables/ facts:

10x table related to place value;

5x table related to 10x table by halving and to the divisions on a clock face;

2x table related to doubling.

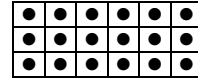
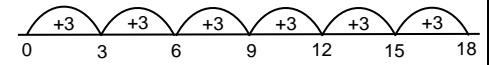
Y3

UxU & TUxU using concrete objects, pictorial representations and mentally

One-digit x one-digit

(model on a number line, 100 square, peg board and using arrays)

$$3 \times 6 = 18$$



One-digit x multiple of ten

(model using a place value slider and base ten)

$$3 \times 50 = 3 \times 5 \times 10$$

$$= 15 \times 10$$

$$= 150$$

Rules of multiplication

Recognise that multiplication can be done in any order:

$$4 \times 12 \times 5 = 4 \times 5 \times 12$$

$$= 20 \times 12$$

$$= 240$$

Multiplication tables

3, 4 and 8 multiplication tables modelled as arrays and repeated addition on a number line and practised using rhythm, songs and games.

Make connections between the tables/ facts:

4x and 8x tables related to the 2x table by doubling;

Commutativity means key facts (2x, 5x, 10x) are already known;

Relate to division facts.

Two-digit x one-digit

(model as an array)

$$23 \times 4 =$$

x	20	3	
4	80	12	80 + 12 = 92

Y4

Grid method for HTUxU, leading to column written method for TUxU and HTUxU

Multiplication tables

6, 12, 9, 7 and 11 multiplication tables modelled as arrays and repeated addition on a number line and practised using rhythm, songs and games.

Make connections between the tables/ facts.

Rules of multiplication

Commutative law:

$$4 \times 12 = 12 \times 4$$

Associative law:

$$(2 \times 3) \times 4 = 2 \times (3 \times 4)$$

Distributive law:

$$39 \times 7 = (30 \times 7) + (9 \times 7)$$

Three-digit x one-digit

(model as an array)

$$146 \times 7 =$$

x	100	40	6
7	700	280	42

$$700 + 280 + 42 = 1022$$

Leading to...

$$146 \times 7 =$$

$$\begin{array}{r} 146 \\ \times 7 \\ \hline 700 \text{ (100 x 7)} \\ 280 \text{ (40 x 7)} \\ \underline{42} \text{ (6 x 7)} \\ 1022 \end{array}$$

Leading to formal short multiplication:

$$146 \times 7 =$$

$$\begin{array}{r} 146 \\ \times 7 \\ \hline 1022 \\ 134 \end{array}$$

Y5

Column written method for HTUxU & ThHTUxU and grid method for TUxTU & HTUxU

Multiplication tables

Continue to practise all multiplication tables facts up to 12 x 12 using counting, rhythm, songs, games and patterns.

Short multiplication

$$4346 \times 8 =$$

$$\begin{array}{r} 4346 \\ \times 8 \\ \hline 34768 \\ 234 \end{array}$$

Also with decimals:

$$4.92 \times 3 =$$

$$\begin{array}{r} 4.92 \\ \times 3 \\ \hline 14.76 \\ 12 \end{array}$$

Long multiplication

(model as an array)

Practise TU x TU and HTU x TU

$$352 \times 24 =$$

x	300	50	2
20	6000	1000	40
4	1200	200	8

$$7040 + 1408 = 8448$$

Y6

Column written method for HTUxTU & ThHTUxTU

Multiplication tables

Continue to practise all multiplication tables facts up to 12 x 12 using counting, rhythm, songs, games and patterns.

Formal long multiplication

Relate to grid method:

$$24 \times 32 =$$

$$\begin{array}{r} 24 \\ \times 32 \\ \hline 48 \text{ (24 x 2)} \\ \underline{720} \text{ (24 x 30)} \\ 768 \end{array}$$

$$352 \times 24 =$$

$$\begin{array}{r} 352 \\ \times 24 \\ \hline 1408 \text{ (352 x 4)} \\ \underline{7040} \text{ (352 x 20)} \\ 8448 \end{array}$$

$$2418 \times 36 =$$

$$\begin{array}{r} 2418 \\ \times 36 \\ \hline 14508 \text{ (2418 x 6)} \\ \underline{72540} \text{ (2418 x 30)} \\ 87048 \end{array}$$